

# YEAR 10 - SIMILARITY...

# Trigonometry

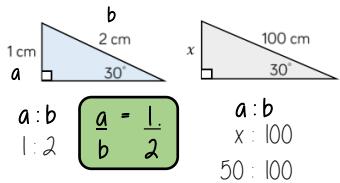
@whisto\_maths

## What do I need to be able to do?

By the end of this unit you should be able to:

- Work fluently with hypotenuse, opposite and adjacent sides
- Use the tan, sine and cosine ratio to find missing side lengths
- Use the tan, sine and cosine ratio to find missing angles
- Calculate sides using Pythagoras' Theorem

## Ratio in right-angled triangles

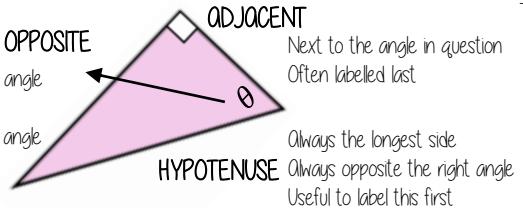


When the angle is the same the ratio of sides  $a$  and  $b$  will also remain the same

$$\begin{aligned} a:b &= \frac{1}{2} \\ 1:2 &= \frac{a}{b} \\ a:b &= x:100 \\ 50:100 &= 0.07:x \\ 0.07:x &= 0.07:0.14 \end{aligned}$$

## Hypotenuse, adjacent and opposite

ONLY right-angled triangles are labelled in this way



Next to the angle in question  
Often labelled last

Always the longest side  
Always opposite the right angle  
Useful to label this first

## Tangent ratio: side lengths

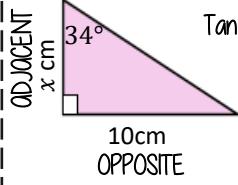
$$\tan\theta = \frac{\text{opposite side}}{\text{adjacent side}}$$

Substitute the values into the tangent formula

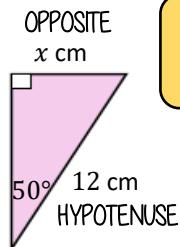
$$\tan 34^\circ = \frac{10}{x}$$

Equations might need rearranging to solve

$$x \times \tan 34^\circ = 10 \\ x = \frac{10}{\tan 34^\circ} = 14.8\text{cm}$$



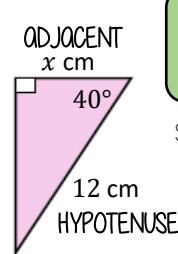
## Sin and Cos ratio: side lengths



$$\sin\theta = \frac{\text{opposite side}}{\text{hypotenuse side}}$$

NOTE

The  $\sin(x)$  ratio is the same as the  $\cos(90-x)$  ratio



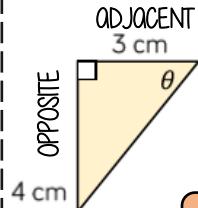
$$\cos\theta = \frac{\text{adjacent side}}{\text{hypotenuse side}}$$

Substitute the values into the ratio formula

Equations might need rearranging to solve

## Sin, Cos, Tan: Angles

### Inverse trigonometric functions



Label your triangle and choose your trigonometric ratio

Substitute values into the ratio formula

$$\theta = \tan^{-1} \frac{\text{opposite side}}{\text{adjacent side}}$$

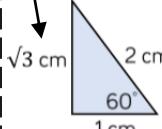
$$\theta = \sin^{-1} \frac{\text{opposite side}}{\text{hypotenuse side}}$$

$$\theta = \tan^{-1} \frac{3}{4} \\ \theta = 36.9^\circ$$

$$\theta = \cos^{-1} \frac{\text{adjacent side}}{\text{hypotenuse side}}$$

## Key angles

This side could be calculated using Pythagoras



Because trig ratios remain the same for similar shapes you can generalise from the following statements

$$\tan 30^\circ = \frac{1}{\sqrt{3}}$$

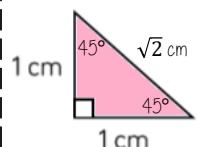
$$\tan 60^\circ = \sqrt{3}$$

$$\cos 30^\circ = \frac{\sqrt{3}}{2}$$

$$\cos 60^\circ = \frac{1}{2}$$

$$\sin 30^\circ = \frac{1}{2}$$

$$\sin 60^\circ = \frac{\sqrt{3}}{2}$$



$$\tan 45^\circ = 1$$

$$\cos 45^\circ = \frac{1}{\sqrt{2}}$$

$$\sin 45^\circ = \frac{1}{\sqrt{2}}$$

## Key angles $0^\circ$ and $90^\circ$

$$\tan 0^\circ = 0$$

~~$$\tan 90^\circ$$~~

This value cannot be defined - it is impossible as you cannot have two  $90^\circ$  angles in a triangle



$$\sin 0^\circ = 0$$

$$\sin 90^\circ = 1$$

$$\cos 0^\circ = 1$$

$$\cos 90^\circ = 0$$