### My mathematical journey

## What do I need to remember from before?

Measuring length, area and volume (NP1)

Area of shapes (GM3)

Types of solids and their nets (GM7)

# What will I learn about in this unit?

Surface area and volume of cubes and cuboids, prisms, cylinders, spheres, pyramids, cones and frustums

Converting between square and cubic units

Surface area and volume of similar solids

#### Where does this lead?

Pythagoras and trigonometry in 3D (GM9)

Solving geometric problems, including density and pressure (GM11)

A Level Mathematics

Construction, engineering and architecture

### Fingertip facts: what I need to learn by heart

The concepts of surface area and volume are the same for all solids, but some have specific formulae to learn.

| Solid    | Surface area (sum of the area of all the faces)   | Volume (space inside the solid)   | Unit conversions   |
|----------|---|---|--|
| Cuboid   |   | length × width × height = lwh   | When converting between square units, we square the length conversion factor.  e.g. 1 m² = 100² cm² = 10 000 cm²  When converting between cubic units, we cube the length conversion factor.  e.g. 1 m³ = 100³ cm³ = 1 000 000 cm³ |
| Prism    |   | area of cross-section<br>× length   |  |
| Cylinder | area of two circles<br>+ curved surface area<br>= $2\pi r^2 + 2\pi rh$<br>= $2\pi r^2 + \pi dh$     | area of cross-section  × length  = $\pi r^2 h$  |  |
| Sphere   | curved surface area $= 4\pi r^2$  | $\frac{4}{3}\pi r^3$  | Similar solids The relationship between scale factors of length (1D), area (2D)  |
| Pyramid  |   | $\frac{1}{3}$ volume of a prism with same base and height                                   | and volume (3D):  Length scale factor, k   Volume scale factor, k  Area scale factor, k²   |
| Cone     | base + curved surface area $= \pi r^2 + \pi r l$  | $\frac{1}{3}$ volume of a cylinder with same base and height $= \frac{1}{3}\pi r^2 h$       |  |
| Frustum  | curved surface area (large cone – small cone) + two circles = $\pi RL - \pi rl + \pi R^2 + \pi r^2$ | volume of large cone – volume of small cone $= \frac{1}{3}\pi R^2 H - \frac{1}{3}\pi r^2 h$ |  |

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